PROBLEM SET: Discounting

Exercise 1. Kangaroo autos (BM 3.10) [3]
Kangaroo Autos is offering free credit on a new $\$ 10,000$ car. You pay $\$ 1,000$ down and then $\$ 300$ a month for the next 30 months. Turtle Motors next door does not offer free credit but will give you $\$ 1,000$ off the list price.

1. If the rate of interest is 10 percent a year, which company is offering the better deal?

## Exercise 2. Bahamas [2]

Suppose you are saving for a trip to the Bahamas in two years and will need $\$ 2000$ at that time. The rate at which you can invest is $10 \%$.

1. How much will you need to invest today to have enough money to make your trip two years from now?

Exercise 3. Project [2]
An investment project offers the following pattern of cash flows.

| Time $(t)$ | Cash Flow $\left(C_{T}\right)$ |
| :---: | ---: |
| 0 | $-\$ 1000$ |
| 1 | 500 |
| 2 | 750 |
| 3 | 250 |

The appropriate discount rate is $10 \%$.

1. What is the NPV of the investment project?

Exercise 4. Investment choices [3]
Suppose the firm has the following investment opportunities:

| Project | Cost | Cash Flow next year |
| :---: | :---: | :---: |
| A | 100,000 | 125,000 |
| B | 200,000 | 260,000 |
| C | 300,000 | 330,000 |
| D | 400,000 | 480,000 |

The firm has $\$ 400,000$ of cash available for investment. The opportunity cost of capital is $15 \%$.

1. Compute the NPV of each project. Which projects should the firm invest in?
2. How much will the firm need to borrow to meet its optimal investment plans if it pays no dividend at $t=0$ ?
3. What dividend will the firm pay to its shareholders next year (at $t=1$ )?
4. What is the current market value of the firms shares?
5. How do your answers to part 1 change if the firms pays it's shareholders a dividend of $\$ 200,000$ at $t=0$ ?

Exercise 5. Arnold's autos. [3]
You are interested in buying a new car. Your car dealer (Arnold's autos) offers to sell you the car for $\$ 10,000$ cash or $\$ 5,000$ per year for the next 3 years. Your banker has agreed to lend you the $\$ 10,000$ to purchase the car if you repay the bank $\$ 499.24$ per month for the next 2 years. Your mother has also agreed to lend you the $\$ 10,000$ if you pay her $\$ 2,000$ per year for 4 years and a balloon payment of $\$ 12,000$ in the fifth year.

1. If these are your only alternatives, what should you do?

Exercise 6. Telephones [5]
Marcus Boruc has been working on a new hands-free telephone that clips into your ear. The new gadget has now been cleared for manufacture and development. Marcus anticipates his first annual cash flow from the phone to be $€ 200,000$, received two years from today. Subsequent annual cash flows will grow at $5 \%$ in perpetuity. What is the present value of the phone if the discount rate is $10 \%$ ?

