## Empirical Methods in Corporate Finance: Event Studies etc

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## 1 Intro

Will cover some of the most important methods for doing empirical research in corporate finance.

## 2 Corporate Events.

Idea: Want to measure the effect of some corporate "event"
Example events:

- Issuing Equity: IPO.
- Issuing Equity: SEO.
- Mergers.
- Issuing Debt.
- ....

How would one measure the effect of such an "event" on the value of a corporation?

### 2.1 Short term price movements.

Suppose we assume that markets are able to rationally assess the information about the event when it is released, and set a new value on the firm that incorporates this information (Impose Semi-Strong Market Efficiency.)
$\rightarrow$ Prices of the firm's securities should adjust immediately the news are public.
$\rightarrow$ The price change on the announcement day is a measure of the effect of the corporate event.

This is the idea behind the traditional event study.
If we see the following behaviour of the stock price around the day when information is released:


We can say that it looks like the market viewed this announcement as positive news. But there may be other causes for the price movement. To control for this, want to average over many companies doing the same thing. Other, unrelated causes for price movements should "average out," and we are left with the effects of the one event we are interested in.

### 2.2 Long term price movements.

What if we are not willing to assume that markets are that rational, or we can not even observe market data before the "event" (such as an IPO)

An alternative: Is it possible to compare the long term return to holding stocks for the company in question with a "control company," a company that is otherwise similar to the "event company," but did not perform the particular action we want to investigate. For example, compare an IPO company with a company already on the exchange, but in the same industry and of the same size.

Suppose we get a picture like the following:


Again, there may be numerous reasons for the differences between the companies, to rule out this average over many companies.

## 3 Traditional event studies

Event studies are one of the mainstays of empirical corporate finance research. The purpose of an event study is to test what Fama (1970) called semi-strong efficiency, that markets react rationally to the release of public information. Most of them are done using the same setup. Lets start by looking at this.

### 3.1 Theoretical background

Efficient market hypothesis (semistrong version)
The market incorporates all public information into setting the current market price.
What happens if the market receives "new" information? The stock price changes to reflect the new information.

Event study - measures the impact of a corporate event. - How big is the change in firm value induced by this shock to information?

The idea
$P_{0}=$ Stock price $=E\left[\left.\sum_{t} \frac{C \text { flow }_{t}}{(1+r)^{t}} \right\rvert\,\right.$ Information at time $\left.t\right]$.
New piece of information
$P_{0}($ new $)=E\left[\left.\sum_{t} \frac{\text { Cflow }_{t}}{(1+r)^{t}} \right\rvert\,\right.$ Information at time $t$, New information $]$.
From this formulation, clear information can be about

1. Future cash flows
2. Discount rate (riskiness)
3. or both

The object of study is the change in price

$$
P_{0}(\text { new })-P_{0}
$$

as a result of this change in information.
An event study aggregates this idea over many similar information "events" in many different firms. To make this comparable over several companies we therfore use returns, the normalized price change

$$
R_{i t}=\frac{P_{0}(n e w)-P_{0}}{P_{0}}
$$

This aggregation also controls for any confounding effects by other news about the company happening at the same date.

The event study is formulated as a hypothesis test. The null hypothesis is that whatever information do not affect the price.

How can we formulate this null given observations of stock returns, $r_{i t}$ the return of stock $i$ at date $t$. The null is not that this return is equal to zero. Any stock will have a positive expected return $E\left[r_{i t}\right]$, even over a very small interval of time, such as a day.

The null is therefore

$$
H_{0}: r_{i t}-E\left[r_{i t}\right]=0
$$

and the alternative hypothesis

$$
H_{A}: r_{i t}-E\left[r_{i t}\right]
$$

Most of the time we do not test this exactly from this formulation, but this is the basis for any event study.

There are two issues that needs to be adressed when implementing the test.

1. Estimation of expected returns.
2. There may be some uncertainty about the dating of the "event," the day information is released to the market.

### 3.2 CAR's, not returns

The solution to the second question is straightforward, let us start with that one.
Define the difference between the daily stock return at date $t$ for company $i$ and the expected return at date $t$ for company $i$ as

$$
\varepsilon_{i t}=r_{i t}-\widehat{E\left[r_{i t}\right]}
$$

We will think of this as a time series with dates centered at the "event date", call this date date zero


Suppose there is no price reaction, then the time series behaviour of this series is something like


Suppose there is an event at date 0 , which is interpreted as positive by the market. Then the stock price will increase, and we have a positive return on that date.


What if you had made a mistake in dating the "event"?
Well, the time series look like


If you just base your inference on what happened at time 0 , you will miss the return at date -2.

The solution to this is simple.
Since each $\varepsilon_{t}$ is mean zero, the sum of them will also be mean zero.
Define the cumulative abnormal return as

$$
C A R_{-k, t}=\sum_{i=-k}^{t} \varepsilon_{i}
$$

Then, for a case of a positive "jump" in the price at the event date, see a behaviour of CAR as

and if there is no price effect (the null), expect a picture like:


Inference can be based on the estimated $C A R$, and tested for whether $C A R \neq 0$, but some care need to be made in the calculation here, the fact that each CAR is the sum of $\varepsilon_{i}$ changes how standard errors should be calculated.

Using $C A R s$ instead of $\varepsilon_{0}$ is thus a way of

### 3.3 Setup

We have a sample of firms where some "event" has happened. This event is observable, and can be determined ex post. The purpose of the standard event study is to look at the effect of this event on the capital markets. As a rule we have a financial model that is supposed to explain the price behaviour of stocks around the event. For example, if the "event" is that the stocks go ex-dividend, in a tax-free world we expect the price to adjust by decreasing by the amount of dividends.

Our financial model is then a prediction about the return at the time of the "event." What is measured is whether the actual returns deviate from the models prediction, which is measured as the "abnormal" return around the time of the event.

The data is a sample of returns defined in "event time:" That is, the returns are viewed as relative to the date of the event. Typically, if we are looking at daily returns, we look at a "window" of say -60 days to +30 days relative to the event in question.


This is then a cross-sectional study (in principle), because we aggregate returns for a number of different events, without taking into account when the event actually happened.

To estimate the the "abnormal return" $A_{t}$ of an event we use cumulative returns. If $\hat{R}_{i t}$ is the model prediction of the return, $R_{t}$ the actual observed return, $\hat{\epsilon}_{i t}=\hat{R}_{i t}-R_{i t}$ is then the abnormal return.

Then we measure the abnormal return $A_{i t}=\sum_{j=-T}^{t} \epsilon_{i j}$. I.e. $A_{i t}$ is the sum of returns summed in event time.

The hypothesis to be tested is then $\mathcal{H}_{0}$ : The average abnormal return equals zero.
The thing remaining is then describing how we measure the abnormal returns. Some of the common examples are:

- Mean adjusted returns:

$$
E\left[R_{i t}\right]=\bar{R}_{i}
$$

the average of all returns for that stock for a long time period. Typically do not include the event period in this averaging.

$$
\epsilon_{i t}=R_{i t}-\bar{R}_{i} .
$$

- Market adjusted returns:

$$
E\left[R_{i t}\right]=R_{m t}
$$

Set the return

$$
\epsilon_{i t}=R_{i t}-R_{m t}
$$

- Market model adjusted returns:

$$
\begin{aligned}
& E\left[R_{i t}\right]=\widehat{\alpha}_{i}+\widehat{\beta}_{i} R_{m t} \\
& \epsilon_{i t}=R_{i t}-\left(\widehat{\alpha}_{i}+\widehat{\beta}_{i} R_{m t}\right)
\end{aligned}
$$

- CAPM adjusted returns:

$$
E\left[R_{i t}\right]=r_{f t}+\left(R_{m t}-r_{f t}\right) \widehat{\beta}_{i}
$$

Here $\beta_{i}$ needs to be estimated, for example from historical data.

$$
\epsilon_{i t}=R_{i t}-\left(r_{f t}+\left(R_{m t}-r_{f t}\right) \widehat{\beta}_{i}\right)
$$

- "Rolling regressions:"

$$
\widehat{E\left[R_{i t}\right]}=\widehat{\gamma}_{0 t}+\widehat{\gamma}_{1 t} \widehat{\beta}_{i t}
$$

where $\beta_{i t}$ has been calculated at time $t$ using data up to date $t$. Note that this is very similar to the market model estimation, there is just a continous updating of the parameters. However, adding one observation at the time will not affect things that much.

$$
\epsilon_{i t}=R_{i t}-\left(\widehat{\gamma}_{0 t}+\widehat{\gamma}_{1 t} \widehat{\beta}_{i t}\right)
$$

- APT adjusted returns

$$
\widehat{E\left[R_{i t}\right]}=r_{f t}+\mathbf{f}^{\prime} \mathbf{b}
$$

- Fama French Adjusted returns

$$
\widehat{E\left[R_{i t}\right]}=r_{f}+\left(E\left[r_{m}\right]-r_{f}\right) \beta_{i}+S M B_{t} b_{s m b, i}+H M L_{t} b_{h m l, i}
$$

After having chosen one of the above ways of measuring abnormal returns, the results of the study is then shown by plotting the averages of the abnormal returns for all the firm in the sample. Figures 1 and 2 represent typical patterns, where the first find that there are positive abnormal returns, and the second show no signs of abnormal returns.

### 3.4 A typical event study

This species of research is best understood by looking at an example, and I have chosen Dann (1981) as one typical example among many possible.

It follows the typical setup (cookbook) for an events study:

- What does the real world look like? (What is the event?)
- What is the theoretical prediction? (Testable hypotheses?).
- Describe setup.
- Sample of firm. Data gathering. Summary statistics.
- How do we measure abnormal returns?

Figure 1 Event Study: typical picture; positive abnormal return.


Figure 2 Typical Picture, no abnormal return.


- Results.
- Graph abnormal returns against event time.
- Test whether effect at time 0 is significant. (t-test with adjustments after taste.
- Discussion.
- If we find significant abnormal return, what can explain it?
- If we don't find a significant return. Will not be published, not observed.

Let us now look at the particulars of Dann (1981). The event of interest: Stock repurchases. We study the effect of announcement of this on stock market prices.

In a perfect market, expect no effect, since this is just a simple exchange of cash for stocks.
Results: Positive abnormal returns.
Possible imperfections that can explain any abnormal return.

- Taxes. A repurchase is taxed as capital gains, different from dividends. Gain to shareholders.
- Signalling. The repurchase is viewed as "good news" about the firm from the point of view of the capital markets.
- Wealth transfer from higher-priority stake-holders (debt) to shareholders. (Net effect on firm is zero.)


### 3.5 Issues that have been studied with event studies.

Some examples of the stuff people have analysed:

- Stock Splits: Fama, Fisher, Jensen, and Roll (1969).
- Stock Redemptions : Dann (1981).
- Capital Structure Changes: Masulis (1980).
- Mergers: Mandelker (1974).
- Proxy Fights: Dodd and Warner (1983).
- New stock issues: Asquith and Mullins (1986), Masulis and Korwar (1986).
- Unexpected dividend changes: Asquith and Mullins (1983).

See Jensen and Ruback (1983) and Jensen and Warner (1988) for overviews of applications to corporate control, and Smith Jr (1986) for an overview of applications to financing decisions.

### 3.6 Simulation evidence.

The Brown and Warner (1985) study is looking at the relative merits of using different adjustments to the mean returns. (Can also be titled an empirical test of the Central Limit Theorem.)

Object of study: What model to use in event studies for finding predicted returns?
Conclusions: It does not really matter much.
Monthly data Brown and Warner (1980): Just use mean-adjusted returns, except when events are clustered in real time.

Daily data: Brown and Warner (1985):

- Just use market adjusted return.
- Not sensitive to non-normal returns.
- Not sensitive to beta-estimation.
- Cross-sectional volatility may be a problem, if there is increased variance at the time of the "event."
Use autocorrelation robust standard errors just to be sure.
Let me summarise the reason for this lack of sensitivity in a simple example. Suppose the true yearly return $R_{i}=25 \%$. If we convert this to daily returns, $\widehat{R}_{i t}=\left(1+\frac{R_{i}}{250}\right)-1=$ $\left(1+\frac{0.25}{250}\right)-1=0.001$. Consider now an estimation error of $10 \%$ in the predicted return, which says $\widehat{R}_{i t} \in(0.0009,0.0011)$.

Suppose we have an event with an abnormal return $A_{i t}$ of $1 \%$ on one day.
Our estimate of the abnormal return is $A_{i t}-\widehat{R}_{i t}=0.01-\widehat{R}_{i t} \in(0.0099,0.0111)$. No matter what kind of prediction error we have, we still get positive estimate of the abnormal return.

The abnormal return "drowns" the estimation error in the predicted returns.

### 3.7 Econometric Issues in traditional event studies.

Brown and Warner (1985) says that in most cases can rely on eyeballing the "jump" at the event date. However, it is necessary to do some econometrics, if only to make the referee happy. And if you want to do something more than just say that the "blip" is there, you need to be more careful.

What are the econometric issues
a) Choose a model for "normal" performance

- Statistical model
- Constant Mean
- Market Model
- Factor Model
- Economic model
- CAPM
- APT
b) Given the model of "normal" performance, measure abnormal performance

1. Estimate parameters of normal performance model in period $T_{0}-T_{1}$ (using textbook notation).
2. Use estimates in calculating abnormal returns.

$$
\hat{\epsilon}_{i t}=R_{i t}-E\left[R_{i t} \mid \text { parameters }\right]
$$

The estimation error in $E\left[R_{i t} \mid\right.$ parameters $]$ due to parameter estimation will affect errors in $\hat{\epsilon}_{i t}$.
3. Aggregate errors into CAR: Cumulative abnormal returns

$$
\widehat{C A R}_{i}\left(\tau_{1}, \tau_{2}\right)=\sum_{t=\tau_{1}}^{\tau_{2}} \hat{\epsilon}_{i t}
$$

Under the null both $\hat{\epsilon}_{i t}$ and $\widehat{\operatorname{CAR}}_{i}\left(\tau_{1}, \tau_{2}\right)$ have expectation zero. With assumptions on the distributions of $\epsilon$ easily tested.

Next Econometric Issue: If we do find an effect, can we do more than just report the "jump" and hypothesize about its causes?

Yes, can try to explain the "jump" from data. The best exposition of this is in the survey by Thompson (1995).

Return generating process

$$
r_{t}=X_{t} B+F G+e
$$

where
$X_{t}$ is the set of variables that go into the "normal returns" process, eg the market return. $B$ is the parameters of this "normal returns" process $F$ is a set of firm characteristics hypothesized to influence the impact of the event on the returns process
$G$ parameters on $F$.
$e$ is an error term
If there is no event, the returns follow the returns generating process

$$
r_{t}=X_{t} B+e
$$

The standard event study in this setup will be to set $F$ to one (the constant).
This setup can be generalized to encompass both event and nonevent periods as

$$
r_{t}=X_{t} B+D \otimes F G+e
$$

where $D$ is an appropriate matrix of zeros and ones, so that non-event periods have zero, and event period have one. (See how you would construct the matrix.)

### 3.8 Practicalities.

Implementation-wise, there are a number of pitfalls to a traditional event study.
The difficult data issue in doing an event study is gathering data about the "event dates." It is necessary to have a reasonable number of events to take averages over. For each event we have to exactly identify the date at which the information became public.

This is not information that is easily available in databases. The traditional method is to get the microfilms of e.g. Wall Street Journal for some years, and, using the index, finding the first mention of the event for each company.

## 4 Selection and other biases in the data and model.

### 4.1 More advanced modelling of the "event:" Self Selection.

The main problem with the standard event study technique appears when the event in question is a choice by the manager/firm. This choice is based on an optimisation by the manager. The model should therefore be estimated on a choice-theoretic basis, taking into account that we only observe the event conditional on it being a positive outcome of the managers optimisation.

The first paper that used this was Acharya (1988). We will look at Eckbo, Maksimovic, and Williams (1990) as an easier application.

### 4.2 Simple example

To see the problem even more clearly than the merger case, consider the following "story".
Suppose the firm has the option to sue somebody for damages, and let this suit be idiosyncratic. Suppose the CAPM holds.

Then the return to the firms stock $r_{i}$ is

$$
r_{i t}=r_{f}+\left(r_{m}-r_{f}\right) \beta_{i}+\varepsilon_{i}+1_{\{\text {suit }\}} r_{\text {suit }}
$$

Here $r_{\text {suit }}$ is the return from the suit, and $1_{\{\text {suit }\}}$ the indicator function for the suit, equal to one if the suit happens, and zero otherwise. $\varepsilon_{i}$ is the usual mean zero error term.

Let us think about estimating $E\left[r_{\text {suit }}\right]$ from an observed sample of court cases.
For simplicity, assume the return from the court case $r_{\text {suit }}$ is either $r_{w}$ if we win, and $r_{l}$ if we lose, and the probability of loosing is $p$. Then $E\left[r_{\text {suit }}\right]=(1-p) r_{w}+p r_{l}$. The expected return is

$$
\begin{aligned}
E\left[r_{i t}\right] & =1 r_{f}+\left(E\left[r_{m}\right]-r_{f}\right) \beta_{i}+E\left[\varepsilon_{i}\right]+1_{\{s u i t\}} E\left[r_{\text {suit }}\right] \\
& =r_{f}+\left(E\left[r_{m}\right]-r_{f}\right) \beta_{i}+1_{\{s u i t\}}\left((1-p) r_{w}+p r_{l}\right)
\end{aligned}
$$

Recall we want to estimate $E\left[r_{\text {suit }}\right]$. However, this is where there is a selection bias. We only observe cases where the decision to press the suit has been made. If this decision is based on better information about the expected outcome, we only observe cases that are more likely to be won than the average case.

Consider the extreme case, the case where the insiders can predict the outcome with certainty. Then, what we estimate for $E\left[r_{\text {suit }}\right]$ will be $r_{w}$ instead of $(1-p) r_{w}+p r_{l}$. There is a bias to the estimated return, because we do not take into account that we are seeing a conditional distribution.

Compare the two regressions

$$
\begin{aligned}
r_{i t} & =r_{f}+\left(E\left[r_{m}\right]-r_{f}\right) \beta_{i}+E\left[r_{\text {suit }}\right]+\varepsilon_{i t} \\
r_{i t} & =r_{f}+\left(E\left[r_{m}\right]-r_{f}\right) \beta_{i}+r_{w}+e_{i t}
\end{aligned}
$$

Subtract the two, solve for $e_{i t}$ :

$$
\begin{aligned}
e_{i t} & =\varepsilon_{i t}+E\left[r_{\text {suit }}\right]-r_{w} \\
E\left[e_{i t}\right] & =\varepsilon_{i t}+(1-p) r_{w}+p r_{l}-r_{w} \\
& =0+p\left(r_{l}-r_{w}\right)<0
\end{aligned}
$$

We do not have $E\left[e_{i t}\right]=0$ in the latter regression, and hence it does not fulfill the usual unbiasedness assumptions. To do estimation, we need to correct this biasedness in the estimates.

### 4.3 Application to mergers

This intuition is what underlies the EMW paper. The event they are analysing is a merger decision. They are assuming that the manager who makes the merger decision is better informed about the value of the merger, and we therefore have the same kind of biasedness in the estimation of the a priori gain to the merger.

Let us now look at the details of the econometric specification. The important part of understanding EMW is section 1, the econometric specification.

Let me go through some of the steps in that section in detail. We are looking at the announcement of a merger between two firms. The important question is to find the predicted return, in order to compare this to the actually observed return.

Let $y_{j}$ be the return on the synergy in the merger, ie. if $v_{j}^{+}$is the return of stock after the merger, and $v_{j}^{-}$the return before, $y_{j}=\ln \left(\frac{v_{j}^{+}}{v_{j}^{-}}\right)$.
$y_{j}$ is partly public and partly private information,

$$
y_{j}=x_{j} \gamma+\eta_{j}
$$

$x_{j}$ is public information, and $\gamma$ are the coefficients in a regression on the public information to predict the value $y_{j}$, i.e. $x_{j} \gamma$ is the public's best prediction of the value of the merger $y_{j}$. Assume this is unbiased, $E\left[x_{j} \gamma\right]=y_{j}$.
$\eta_{j}$ is some private information with mean zero.
In order to find the public estimate of the expected return of a stock, consider

$$
r_{i t}=\alpha_{j}+\beta_{j} r_{m t}+1_{\{j t\}} x_{j} \gamma+\epsilon_{j t}
$$

We need to estimate the coefficients $\gamma$. If we had a random sample of firms, this would not be a problem, we would run the above regression.

However, the fact that we only observe this for firms that announce a merger, creates a selection bias in $1_{\{j t\}}$, this is a function of the private information of the manager. Hence $1_{\{j t\}}$ will be correlated with the error term, and estimation will be biased.

We need to replace $1_{\{j t\}} x_{j} \gamma$ above with something that restores the consistency.
Consider the private information $\eta_{j}$.
The insiders will only choose to merge if the gain $y_{j}$ to the merger is positive, $y_{j}>0$.
Using the private info, the condition is

$$
y_{j}=x_{j} \gamma+\eta_{j}>0,
$$

or

$$
\eta_{j}>-x_{j} \gamma
$$

Conditional on observing a merger offer, the public's best estimate of the value of the merger is then

$$
E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]
$$

Replace $x_{j} \gamma$ with $E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]$ in the regression above:

$$
r_{i t}=\alpha_{j}+\beta_{j} r_{m t}+1_{\{j t\}} E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]+\zeta_{j t}
$$

The error term $\zeta_{j t}$ here fulfills all conditions for estimation,

$$
E\left[\zeta_{j t}\right]=0
$$

$$
E\left[\zeta_{j t} x_{j t}\right]=0
$$

This is then the public best prediction of the true value of the merger. This is what the observed value should be measured against to get the abnormal return.

The problem is then to find $E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]$. That is the hard part, to find the public's prediction of the value of the merger.

To do this EMW makes distributional assumptions in order to apply Maximum Likelihood. Assume that $\eta_{j}$, the private information, has mean zero, and is normally distributed with variance $\omega$.

This is enough assumptions to actually estimate the conditional expectation above. It is shown in the paper that we can replace $E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]$ with $F\left(x_{j}\right)=x_{j} \gamma+\frac{n\left(z_{j}\right)}{N\left(z_{j}\right)}$, where
$n(\cdot)$ is the unit normal distribution function,
$N(\cdot)$ the cumulative normal distribution function and $z_{j}=\frac{x_{j} \gamma}{\omega}$.

This part is a bit hard to follow, so let me go through the derivation in detail, since the rest follows easily once you see how to get this.

We use some useful properties of the normal distribution: ${ }^{1}$ Let $z$ have a unit normal distribution.

$$
\begin{aligned}
& z \sim N(0,1) \\
& \begin{aligned}
& n(z)=\frac{1}{\sqrt{2 \pi}} e^{-\frac{1}{2} z^{2}} \\
& N(z)=\int_{-\infty}^{z} \frac{1}{\sqrt{2 \pi}} e^{-\frac{1}{2}^{2}} d x \\
& \begin{aligned}
N(-z)=1-N(z)
\end{aligned} \\
& \begin{aligned}
E[z \mid z>x] & =\frac{1}{P(z>x)} \int_{x}^{\infty} z n(z) d z \\
& =\frac{1}{1-N(x)} \int_{x}^{\infty} z n(z) d z \\
& =\frac{1}{N(-x)} \int_{x}^{\infty} z n(z) d z \\
& =\frac{1}{N(-x)} \int_{x}^{\infty}-\frac{d}{d z} n(z) d z \\
& =\frac{1}{N(-x)}[n(\infty)-n(x)] \\
& =\frac{1}{N(-x)}[0+n(-x)] \\
& =\frac{n(-x)}{N(-x)}
\end{aligned}
\end{aligned}>=\begin{array}{l}
n
\end{array}
\end{aligned}
$$

Then, we have the tools to evaluate

$$
E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]=E\left[x_{j} \gamma+\eta_{j} \mid \eta_{j}>-x_{j} \gamma\right]
$$

[^0]The first thing we need to do is to get a unit normal, in order to use the trick above. Divide through by the variance $\omega$ :

$$
\begin{aligned}
E & {\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right] E\left[x_{j} \gamma+\eta_{j} \mid \eta_{j}>-x_{j} \gamma\right] } \\
& =E\left[x_{j} \gamma+\eta_{j} \left\lvert\, \frac{\eta_{j}}{\omega}>\frac{-x_{j} \gamma}{\omega}\right.\right] \\
& =E\left[x_{j} \gamma \left\lvert\, \frac{\eta_{j}}{\omega}>\frac{-x_{j} \gamma}{\omega}\right.\right]+E\left[\eta_{j} \left\lvert\, \frac{\eta_{j}}{\omega}>\frac{-x_{j} \gamma}{\omega}\right.\right] \\
& =x_{j} \gamma E\left[1 \left\lvert\, \frac{\eta_{j}}{\omega}>\frac{-x_{j} \gamma}{\omega}\right.\right]+\omega E\left[\frac{\eta_{j}}{\omega} \left\lvert\, \frac{\eta_{j}}{\omega}>\frac{-x_{j} \gamma}{\omega}\right.\right] \\
& =x_{j} \gamma \frac{1}{1-N\left(\frac{x_{j} \gamma}{\omega}\right)} \int_{\frac{-x_{j} \gamma}{\omega}}^{\infty} n(z) d z+\omega \frac{n\left(\frac{x_{j} \gamma}{\omega}\right)}{N\left(\frac{x_{j} \gamma}{\omega}\right)} \\
& =x_{j} \gamma \frac{1}{N\left(-\frac{x_{j} \gamma}{\omega}\right)} N\left(\frac{-x_{j} \gamma}{\omega}\right)+\omega \frac{n\left(\frac{x_{j} \gamma}{\omega}\right)}{N\left(\frac{x_{j} \gamma}{\omega}\right)} \\
& =x_{j} \gamma+\omega \frac{n\left(\frac{x_{j} \gamma}{\omega}\right)}{N\left(\frac{x_{j} \gamma}{\omega}\right)} \\
& =x_{j} \gamma+\omega \frac{n\left(z_{j}\right)}{N\left(z_{j}\right)}
\end{aligned}
$$

where $z_{j}=\frac{x_{j} \gamma}{\omega}$.
To summarise, to estimate the predicted return of a stock $i$, we look at

$$
r_{i t}=\alpha_{i}+\beta_{i} r_{m t}+1_{\{j t\}} F\left(x_{j}\right)+\zeta_{i}
$$

where

$$
F\left(x_{j}\right)=x_{j} \gamma+\omega \frac{n\left(z_{j}\right)}{N\left(z_{j}\right)}
$$

As a further refinement to this analysis, we add the possibility of information leakage. Suppose there is a rumour about the possible merger. Conditional on the rumour, the market will reasess the gains from a merger as

$$
\begin{aligned}
E\left[y_{j} \mid x_{j}\right] & =E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right] P\left(\eta_{j}>-x_{j} \gamma\right) \\
& =E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right] N\left(z_{j}\right) \\
& =F\left(x_{j}\right) N\left(z_{j}\right)
\end{aligned}
$$

The abnormal return from the merger is then adjusted for the public change in the estimated merger gain:

$$
\begin{aligned}
G\left(x_{j}\right) & =E\left[y_{j} \mid \eta_{j}>-x_{j} \gamma\right]-E\left[y_{j} \mid x_{j}\right] \\
& =F\left(x_{j}\right)-F\left(x_{j}\right) N\left(z_{j}\right) \\
& =F\left(x_{j}\right)\left(1-N\left(z_{j}\right)\right)
\end{aligned}
$$

And we get a different formulation of the predicted return

$$
r_{i t}=\alpha_{i}+\beta_{i} r_{m t}+1_{\{j t\}} G\left(x_{j}\right)+\zeta_{i}
$$

This is then the econometric issues in the paper. We have found a functional form $F(\cdot)$ (or $G(\cdot)$ ) that allows us to estimate the parameters $\omega$ in the regression $x_{j} \omega$. (Remember those were the parameters of interest.)

The estimation in the paper will use a likelihood function for the errors to estimate the parameters $\gamma, \alpha_{j}$ and $\beta_{j}$.

The remaining issues in the paper is to specify what variables $x_{j}$ is used to predict the merger value, and to be more specific about the exact sequence of the merger announcements. But the big issue is the selection bias, which has been dealt with in the above.

The remainder of the paper is then an investigation of a set of observed mergers. I will not cover those results here in detail, but we do find that there is a significant difference between the ML specification used here and an OLS estimation of the parameters $\omega$. The ML specification is higly significant, whereas the OLS specification was not significant.

## 5 Long term performance.

### 5.1 Long term price movements.

What if we are not willing to assume that markets are that rational, or we can not even observe market data before the "event" (such as an IPO)

An alternative: Is it possible to compare the long term return to holding stocks for the company in question with a "control company," a company that is otherwise similar to the "event company," but did not perform the particular action we want to investigate. For example, compare an IPO company with a company already on the exchange, but in the same industry and of the same size.

Suppose we get a picture like the following:


Again, there may be numerous reasons for the differences between the companies, to rule out this average over many companies.

### 5.2 Start

A more recent phenomen, but also currently used a lot in analyzing corporate finance events, is measurement of long term performance. An early and typical paper in this literature is Loughran and Ritter (1995)'s study of new issues.

A more recent work in the area is Eckbo, Masulis, and Norli (1998).

### 5.3 Basic idea.

Event studies: Measure short-term reactions to corporate "events"
Are there alternative ways to measure market reactions to cross-sectional differences between firms?

Basic idea: Want to investigate difference between two groups of firms:

- Firms doing something.
- Firms not doing it.

A typical example: Firms issuing/not issuing equity.
Then

- Find all firms "doing something".
- For each of these, find a "matching" firm, a firm "not doing that something," but otherwise a firm with similar risk characteristics (and hence similar expected return)
consider then
$E\left[r_{i}\right]$, the expected return on a firm "doing something", and
$E\left[r_{i}^{m}\right]$, the expected return on a firm "not doing something" but with similar risk characteristics as firm $i$.

If the "doing/not doing something" has no effect, and the "matched firm" has similar risk characteristics, it will be the case that

$$
\frac{1+E\left[r_{i}\right]}{1+E\left[r_{i}^{m}\right]}=1
$$

and

$$
E\left[r_{i}\right]-E\left[r_{i}^{m}\right]=0
$$

These are the testable implications.
What is long run? in this context: If we aggregate over longer periods, may get more powerful tests, because the market has "longer" to realize the differences.

So, if $R_{i}$ and $R_{i}^{m}$ are five year aggregations of respectively $r_{i}$ and $r_{i}^{m}$, can still test versions of the above nulls

$$
\begin{aligned}
& \frac{1+E\left[R_{i}\right]}{1+E\left[R_{i}^{m}\right]}=1 \\
& E\left[R_{i}\right]-E\left[R_{i}^{m}\right]=0
\end{aligned}
$$

Conceptually, long run tests are simple. The problem with them is the old saw about the "devil being in the details." It is problematic to have a lot of confidence in them, when they are so sensitive to implementation.

### 5.4 Implementation.

Important issues in implementation of these tests:

- How do we find a "matching" firm?
- How do we measure the economic significance of differences in long term returns?


### 5.4.1 How to find a matching firm.

Turns out to be important for the results. Option used by Loughran and Ritter (1995): Pick the firm with the closest market capitalization to firm $i$.

Criticized for this choice, other peple argued for various alternatives

- industry
- size and industry
- beta
- fama french factors

While this kind of thing was not important for short term event studies, in the long term they are important.

### 5.4.2 Implementation of test for economic significance

Standard statistical issue: Estimation of variance to test significance of mean differences.
But also: Should one strive for what looks like a feasible "trading strategy"?

### 5.5 Interpretation of tests.

Turns out to be significant differences in many cases, but very dependent on design.
Issues to worry about

- Self Selection Biases? Choice to "do something" not random.
- Survival?


## 6 The MacKinlay Survey

For doing event studies these days it is only necessary to grab for the "cookbook" provided by MacKinlay (1997)

Readings Some literature used in the discussion above

-     * Textbook: CLM 4.
- Surveys: Thompson (1995).
- Traditional event studies: Dann (1981), Brown and Warner (1985).
-     * Model of self selection: Eckbo et al. (1990).
- Long term performance: Loughran and Ritter (1995), Eckbo et al. (1998).

Further Reading For textbook treatments of the econometrics of choice theoretical models look at (Amemiya, 1985, Chapter 9) and (Davidson and MacKinnon, 1993, Chapter 15).

Survivorship bias: Brown, Goetzmann, Ibbotson, and Ross (1992).
Event induced variance: Boehmer, Musumeci, and Poulsen (1991)

## References

Acharya. A generalized econometric model of signalling. Journal of Finance, 43, 1988.
Takeshi Amemiya. Advanced Econometrics. Harvard University Press, 1985.
Paul Asquith and David W Mullins. The impact of initiating dividend payments on shareholders' wealth. Journal of Business, 56:77-96, 1983.

Paul Asquith and David W Mullins. Equity issues and offering dilutions. Journal of Financial Economics, 15: 61-89, 1986.

E Boehmer, Jim Musumeci, and A B Poulsen. Event-study methodology under conditions of event-induced variance. Journal of Financial Economics, 30:253-72, 1991.

S J Brown, W Goetzmann, R G Ibbotson, and S A Ross. Survivorship bias in performance studies. Review of Financial Studies, 5(4):553-80, 1992.

Stephen J Brown and Jerold B Warner. Measuring security price performance. Journal of Financial Economics, 8:205-58, 1980.

Stephen J Brown and Jerold B Warner. Using daily stock returns. the case of event studies. Journal of Financial Economics, 14:3-31, 1985.

Larry Y Dann. Common stock repurchases. An analysis of returns to bondholders and stockholders. Journal of Financial Economics, 9:113-38, 1981.

Russel Davidson and James G MacKinnon. Estimation and Interference in Econometrics. Oxford University Press, 1993.

Peter Dodd and Jerold B Warner. On corporate governance: A study of proxy contests. Journal of Financial Economics, 11:401-38, 1983.

B Espen Eckbo, V Maksimovic, and Joseph Williams. Consistent estimation of cross-sectional models in event studies. Review of Financial Studies, 3(3):343-65, 1990.

B Espen Eckbo, Ronald W Masulis, and Øyvind Norli. Conditional performance following security offerings: Is there a 'new issues puzzle'? Unpublished Working Paper, May 1998.

Eugene Fama, L Fisher, M Jensen, and Richard Roll. The adjustment of stock prices to new information. International Economic Review, 10:1-21, 1969.

Eugene F Fama. Efficient capital markets: A review of theory and empirical work. Journal of Finance, 25: 383-417, 1970.

Michael C Jensen and Richard S Ruback. The market for corporate control: The scientific evidence. Journal of Financial Economics, 11:5-50, 1983.

Michael C Jensen and Jerold B Warner. The distribution of power among corporate managers, shareholders and directors. Journal of Financial Economics, 20:3-24, 1988.

Tim Loughran and Jay R Ritter. The new issues puzzle. Journal of Finance, 50(1):23-51, March 1995.
A Craig MacKinlay. Event studies in economics and finance. Journal of Economic Literature, XXXV:13-39, March 1997.

Gershon Mandelker. Risk and return: The case of the merging firm. Journal of Financial Economics, 1:303-36, 1974.

Ronald W Masulis. The effect of capital structure change on security prices. Journal of Financial Economics, 8: 139-178, 1980.

Ronald W Masulis and Ashok W Korwar. Seasoned equity offerings: An empirical investigation. Journal of Financial Economics, 15:91-118, 1986.

Clifford W Smith Jr. Investment banking and the capital acquisition process. Journal of Financial Economics, 15:3-29, 1986.

R Thompson. Empirical methods of event studies in corporate finance. In R A Jarrow, V Maksimovic, and W T Ziemba, editors, Finance, volume 9 of Handbooks in Operations Research and Management Science, chapter 29, pages 963-992. North-Holland, 1995.


[^0]:    ${ }^{1}$ If you don't apply these useful formulas, expect to spend a good time trying to get equation (2) in the paper. Shows you that footnotes are useful at times.

